

# 9.3

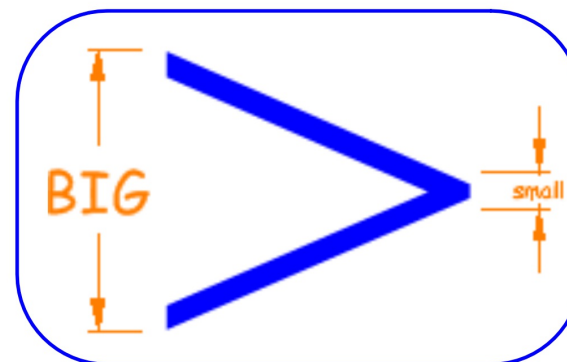
## Solving Linear Inequalities

Objective:

- To solve simple inequalities
- To solve compound inequalities

### Inequalities Symbols:

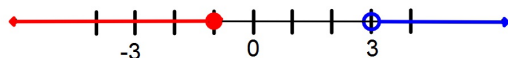
$<$	$>$	$\leq$	$\geq$
less than	greater than	less than or equal to	greater than or equal to



The **graph** of an inequality consists of all points on a real number line that correspond to solutions of the inequality

Graph of  $x \leq -1$

Graph of  $x > 3$



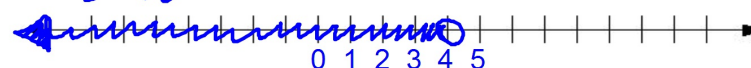
When graphing inequalities on a number line, we use an open dot for  $>$  or  $<$  and a closed dot for  $\leq$  or  $\geq$

Solve an inequality the same as an equation except:  
*If you multiply or divide by a negative number, switch the direction of the inequality sign.*

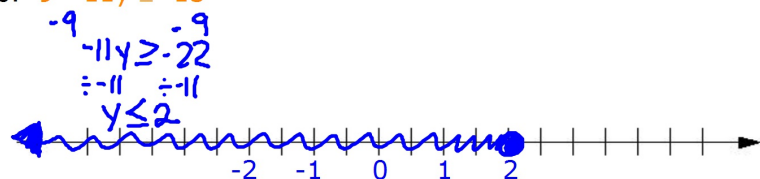
### Example 1: Graphing Inequalities on a number line.

a.  $5y - 8 < 12$

$$\begin{array}{rcl} & +8 & +8 \\ 5y & < & 20 \\ \div 5 & & \div 5 \end{array} \quad y < 4$$



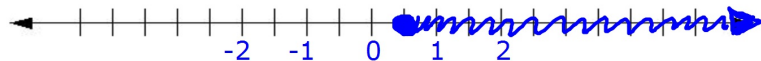
b.  $9 - 11y \geq -13$



c.  $2x + 1 \leq 6x - 1$

$$\begin{array}{r} -2x \quad -2x \\ 1 \leq 4x - 1 \\ +1 \quad +1 \\ 2 \leq 4x \end{array}$$

$$\begin{array}{r} \frac{2}{4} \leq x \\ \frac{1}{2} \leq x \end{array}$$



### Example 2: Checking Solutions.

Decide whether the given number is a solution of the inequality.

$$2x + 1 \leq 6x - 1; x = 3$$

$$\begin{array}{r} 2(3) + 1 \leq 6(3) - 1 \\ 7 \leq 17 \\ \text{yes!} \end{array}$$

Homework: 1.6 Practice A (1,4,5,6,7-11,13-21,28-33)

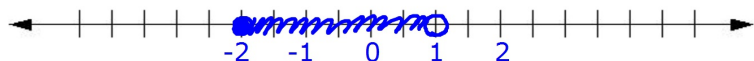
The rest will be assigned tomorrow!

A **compound inequality** is two simple inequalities joined by "and" or "or".

### Example 3: Graphing AND Compound Inequalities.

a)  $-2 \leq x < 1$

(This is read as "x is in between -2 and 1)



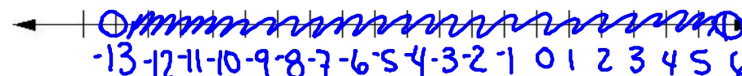
b)  $-2 \leq 3t - 8 \leq 10$

$$\begin{array}{r} +8 \quad +8 \quad +8 \\ 6 \leq 3t \leq 18 \\ \div 3 \quad \div 3 \quad \div 3 \\ 2 \leq t \leq 6 \end{array}$$



c)  $-9 < t + 4 < 10$

$$\begin{array}{r} -4 \quad -4 \quad -4 \\ -13 < t < 6 \end{array}$$



**Example 4: Graphing OR Compound Inequalities.**

a)  $2x + 3 < 5$  or  $4x - 7 \geq 9$

$$\begin{array}{rcl} \underline{-3 \quad -3} & & \underline{+7 \quad +7} \\ 2x < 2 & & 4x \geq 16 \\ \div 2 \quad \div 2 & & \div 4 \quad \div 4 \\ x < 1 & \text{OR} & x \geq 4 \end{array}$$



b)  $6x + 9 < 3$  or  $3x - 8 > 13$

$$\begin{array}{rcl} \underline{-9 \quad -9} & & \underline{+8 \quad +8} \\ 6x < -6 & & 3x > 21 \\ \div 6 \quad \div 6 & & \div 3 \quad \div 3 \\ x < -1 & \text{OR} & x > 7 \end{array}$$

